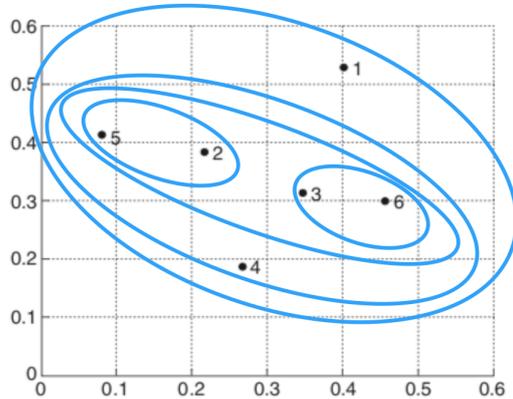


Consider the following points in the 6-dimensional space and the corresponding pairwise distance between these points.



| | p1 | p2 | p3 | p4 | p5 | p6 |
|----|------|------|------|------|------|------|
| p1 | 0.00 | 0.24 | 0.22 | 0.37 | 0.34 | 0.23 |
| p2 | 0.24 | 0.00 | 0.15 | 0.20 | 0.14 | 0.25 |
| p3 | 0.22 | 0.15 | 0.00 | 0.15 | 0.28 | 0.11 |
| p4 | 0.37 | 0.20 | 0.15 | 0.00 | 0.29 | 0.22 |
| p5 | 0.34 | 0.14 | 0.28 | 0.29 | 0.00 | 0.39 |
| p6 | 0.23 | 0.25 | 0.11 | 0.22 | 0.39 | 0.00 |

Apply agglomerative hierarchical clustering on this example using the min distance as a cluster similarity. Compute the proximity matrix over each iteration.

We notice that the smallest distance in the above matrix is between points 3 and 6, therefore we will assign the two in the same cluster and update the distance matrix as follows:

| | 1 | 2 | {3, 6} | 4 | 5 |
|--------|------|------|--------|------|------|
| 1 | 0 | 0.24 | 0.22 | 0.37 | 0.34 |
| 2 | 0.24 | 0 | 0.15 | 0.20 | 0.14 |
| {3, 6} | 0.22 | 0.15 | 0 | 0.15 | 0.28 |
| 4 | 0.37 | 0.20 | 0.15 | 0 | 0.29 |
| 5 | 0.34 | 0.14 | 0.28 | 0.29 | 0 |

Points 2 and 5 have the smallest distance, therefore the new distance matrix becomes as follows:

| | 1 | {2, 5} | {3, 6} | 4 |
|--------|------|--------|--------|------|
| 1 | 0 | 0.24 | 0.22 | 0.37 |
| {2, 5} | 0.24 | 0 | 0.15 | 0.20 |
| {3, 6} | 0.22 | 0.15 | 0 | 0.15 |
| 4 | 0.37 | 0.20 | 0.15 | 0 |

Cluster {2, 5} and cluster {3, 6} have the smallest distance, therefore the new distance matrix becomes as follows:

| | 1 | {2, 5, 3, 6} | 4 |
|--------------|------|--------------|------|
| 1 | 0 | 0.22 | 0.37 |
| {2, 5, 3, 6} | 0.22 | 0 | 0.15 |
| 4 | 0.37 | 0.15 | 0 |

Cluster {2, 5} and cluster {3, 6} have the smallest distance, therefore the new distance matrix becomes as follows:

| | 1 | {2, 5, 3, 6} | 4 |
|--------------|------|--------------|------|
| 1 | 0 | 0.22 | 0.37 |
| {2, 5, 3, 6} | 0.22 | 0 | 0.15 |
| 4 | 0.37 | 0.15 | 0 |

We finally merge cluster {2, 5, 3, 6} with point 4:

| | 1 | {2, 5, 3, 6, 4} |
|-----------------|------|-----------------|
| 1 | 0 | 0.22 |
| {2, 5, 3, 6, 4} | 0.22 | 0 |

Below is the resulting dendrogram for this example:

